Each answer should be a number,  $\infty$ ,  $-\infty$ , or DNE (only if the other answers do not apply).

[a] 
$$\lim_{x \to \infty} \frac{3}{1 - 4 \tan^{-1} x}$$
$$= \frac{3}{1 - 4 \left(\frac{\pi}{2}\right)}$$
$$= \left| \frac{3}{1 - 2\pi} \right| \boxed{1}$$

$$\lim_{x \to 0^+} \frac{2 - x}{1 - e^x} \qquad \frac{2}{O}$$

[b] 
$$\lim_{x \to -\infty} \frac{\sqrt{7x^{10} - x}}{13x^3 + 2x^5} \cdot \frac{\frac{1}{x^5}}{\frac{1}{x^5}}$$

$$= \lim_{x \to -\infty} \frac{\sqrt{7x^{10} - x}}{13x^3 + 2x^5} \cdot \frac{-\sqrt{10}}{\frac{1}{x^5}}$$

$$= \lim_{x \to -\infty} \frac{\sqrt{7x^{10} - x}}{13x^3 + 2x^5} \cdot \frac{-\sqrt{10}}{\frac{1}{x^5}}$$

$$= \lim_{x \to -\infty} \frac{-\sqrt{7} - \frac{1}{x^6}}{\frac{1}{x^5}}$$

$$= -\frac{\sqrt{7} - 0}{0 + 2}$$

Let 
$$f(x) = \sqrt{x^2 + 7}$$
.

[a] Find 
$$f'(x)$$
.

$$\lim_{h\to 0} \frac{\int (x+h)^2 + 7}{h} - \int \chi^2 + 7$$

$$\frac{\int (x+h)^{2}+7}{\sqrt{(x+h)^{2}+7}} + \sqrt{x^{2}+7}$$

$$h > 0$$
  $h \sqrt{(x+h)^2 + 7} + \sqrt{x^2 + 7}$ 

$$\lim_{h\to 0} \frac{(x+h)^2+7-(x^2+7)}{h(x+h)^2+7+\sqrt{x^2+7}} = \lim_{h\to 0} \frac{2x+h}{\sqrt{(x+h)^2+7}+\sqrt{x^2+7}}$$

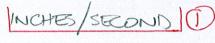
$$\lim_{h\to 0} \frac{2xh+h^2}{h(\sqrt{(x+h)^2+7}+\sqrt{x^2+7})} = \frac{2x}{2\sqrt{x^2+7}} = \frac{x}{\sqrt{x^2+7}}$$
Find the slope-point form of the equation of the tangent line to the curve of  $f(x)$  at the point where  $x=3$ 

Find the slope-point form of the equation of the tangent line to the curve of 
$$f(x)$$
 at the point where  $x = 3$ .

$$f'(3) = \frac{3}{\sqrt{3+7}} = \frac{3}{4}$$

$$y-4=\frac{3}{4}(x-3)$$

The position (in inches) of an object moving in along a line is given by  $s(t) = \sqrt{t^2 + 7}$ , where t is the time in seconds. [c] Find the instantaneous velocity of the object at time t = 2. Give the correct units for your answer.



	span of a certain lightbulb depends on how many hours per day it is switched on. e $L = f(u)$ , where $L$ is the lifespan of the lightbulb, in months, and $u$ is how many hours per day it is a	SCORE:switched on.	/ 2 PTS
[a]	What does $f'(5) = -1$ mean? Your answer must use all the numbers from that equation, and the correct	ct units for those	numbers.
[b]	IF A LIGHTBULB IS SWITCHED ON 5 HOURS A DAY, ITS LIFESPAN IS SHOPTENED BY I MONTH FOR EACH ADDITIONAL HOUR IT IS ON EACH D. Is there a value $u_0$ such that $f'(u_0) > 0$ ? Why or why not?	AY	ADED BY ME
	NO, LEAVING THE LIGHTBULB ON LONGER & WILL ALWAYS CAUSE IT TO HAVE A SHOP	ACH DAY	1 ZESPAN

Using complete sentences & proper mathematical notation, write the formal definition of "derivative (function)". THE DERIVATIVE OF A FUNCTION f IS f'(x) = lim Using complete sentences & proper mathematical notation, write the formal definition of "continuous (at a point)". SCORE: A FUNCTION & IS CONTINUOUS AT a IF f(a) EXISTS, lim f(x) EXISTS AND lim f(x) = f(a) GRADED BY ME

Determine if the function below is continuous at x = -1.

State your conclusion clearly, and show whether each condition in the definition of "continuous" is true or false.

In addition, if it is not continuous, determine the type of discontinuity and justify using the appropriate definition

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$$f(x) = \begin{cases} x - x^4 + x^5, & \text{if } x < -1 \\ -1, & \text{if } x = -1 \\ x^7 - x^2 - 1, & \text{if } x > -1 \end{cases}$$

Not continuous  $\begin{cases} x - x^4 + x^5, & \text{if } x < -1 \\ -1, & \text{if } x = -1 \\ x^7 - x^2 - 1, & \text{if } x > -1 \end{cases}$ 

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